

Calculus AB

5-1

The Natural Logarithm: Differentiation

Algebraic Definition of Logarithm -

Given: $x^b = y \Rightarrow$

Definition of the Number e -

Algebraic Definition of the Natural Logarithm -

Calculus Definition of the Natural Logarithm Function -

Laws of Exponents

Laws of Logarithms -

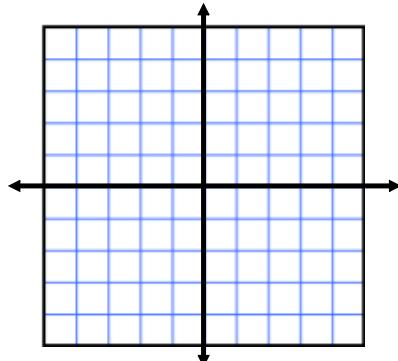
1) $x^m \cdot x^n =$	1)
2) $\frac{x^m}{x^n} =$	2)
3) $(x^m)^n =$	3)

Function Properties: $f(x) = \ln(x)$

Domain:

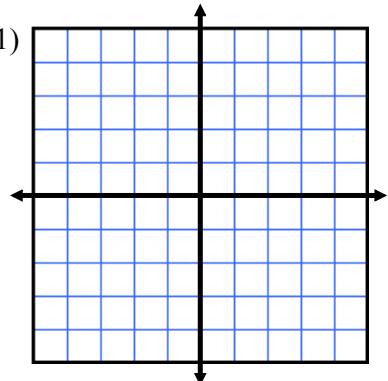
Range:

Asymptotes:



Sketch the graph of the function and state its domain. (pg 331)

12) $f(x) = -2 \ln(x)$



Use the properties of logarithms to expand the logarithmic expression.

22) $\ln \sqrt{x^5}$

24) $\ln(xyz)$

*) $\ln \sqrt[3]{a^2 + 1}$

Write the expression as a logarithm of a single quantity.

30) $\ln x + 2 \ln y - 4 \ln z$

34) $2[\ln x - \ln(x+1) - \ln(x-1)]$

Find the limit.

40) $\lim_{x \rightarrow 6^-} \ln(6-x)$

Assignment
Day 1
pg 331
7-17 odd,
21-35 odd
39-75 odd

Derivative of the Natural Logarithm Function -

Find the derivative of the function.

50) $h(x) = \ln(2x^2 + 1)$

56) $y = \ln \frac{2x}{x+3}$

70) $y = \ln |\csc x|$

Find an equation of the tangent line to the graph of f at the indicated point.

$$78) f(x) = 4 - x^2 - \ln\left(\frac{1}{2}x + 1\right), \quad (0, 4)$$

Show that the function is a solution of the differential equation.

$$90) x \ln x - 4x ; \quad x + y - xy' = 0$$

Locate any relative extrema and inflection points.

$$92) y = x - \ln x$$

Assignment
Day 2
83 - 95 odd